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Price, sales, and the business cycle: Microeconomic evidence \star

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ABSTRACT

This paper uses a rich weekly price database from the largest supermarket in Uruguay to analyze the relationship among prices, micro-level sales, and business cycle conditions. On average, 7% of products were on sale each month, and we show a positive and statistically significant but small relationship between sales and unemployment at the aggregate level, controlling for product and time effects. For each product category, there is a high and positive statistically significant association for these variables. Also, for some categories like food products, alcoholic drinks, beverages, and fruits and vegetables, we found a large, negative, and statistically significant relationship between the probability of being on sale and employment. The mechanism we tested is the following: As the economy worsens and unemployment rises (and/or employment falls), the supermarket uses sales to adjust prices while keeping reference prices fixed. Our results indicate that sales do not alleviate much of the price rigidity in economic recessions.

We also studied sales behavior through a principal component analysis in the time domain. This analysis revealed that the first two principal components explained more than half of each sector's variance in price dynamics. These components are significantly correlated with variations in unemployment and employment. Additionally, we found that movement in the principal components across sectors systematically Granger-cause employment changes.

1. Introduction

Departing from the works of Lucas (1972), Taylor (1979, 1980), and Calvo (1983), the macroeconomic literature has emphasized how microanalyses of price setting are important to understanding the nature of price rigidity, consistency across models, and, more generally, how monetary policy affects the business cycle. In the new Keynesian model of Galí (2008), price rigidity is relevant to explain monetary policy's real effects on output. The seminal work of Blinder (1991) was followed by literature that estimated the degree of price rigidity (Bils and Klenow (2004), Klenow and Malin (2010), Nakamura and Steinsson (2008), Nakamura and Steinsson (2013) and Klenow and Kryvtsov (2008)). Thus, the concern has become quantifying and modeling the degree of price rigidity.

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As new micro-databases have become available (micro CPI data, scanner data, Web scraping, etc.), the most recent literature has started to analyze the relationship between prices and the business cycle at the micro-level. In particular, there has been much discussion on how the prices relate to the economic cycle and how the price variations at the micro-level are related to macroeconomic variables such as unemployment (Coibion et al. (2015), Gagnon et al. (2017), Kryvtsov and Vicent (2021), and Anderson et al. (2017)).

In this context, it is often argued (e.g., Nakamura and Steinsson (2008), Coibion et al. (2015)) that sales (temporarily price reductions) are a channel for price adjustments. Firms can use them to change effective prices while keeping sticky reference prices. However, the empirical work had difficulty defining sales because not all price reductions are sales. Nakamura and Steinsson (2008) use an algorithm to define sales and find that they are an important source of price changes in the US. Traditionally, sales have not been considered from a macro point of view because they are not related to aggregate phenomena.

Our work make two contributions. First, we used a weekly dataset of retail prices from Uruguay to characterize prices' rigidity, the behavior of sales, and their relationship with local market conditions like labor market indicators. In our micro-dataset, the supermarket reports whether the product is on sale or not, so an algorithm is not necessary to identify it. Moreover, sales might not be associated with price reductions (e.g., a sale may be associated with mailed advertising or bundling).

Second, we perform a novel time-series principal component analysis (PCA) to explore the relationships between sales and employment/unemployment, and to study the correlations between the prices of different products in each sector. To the best of our knowledge, this paper is the first to use this methodology to study price rigidity. PCA is used to reduce dimensionality while retaining as much variation as possible¹ In this case, we extracted two time series for each category of products in our dataset – the first and second principal components (PCs) – which are representative of the price dynamics of the *whole* category, as testified by the fact that such two time series account for about 45% to 65% of the variation in price, depending on the product category. This, in turn, provides a very parsimonious description of the price dynamics in each sector, which we leverage to explore the relationship between prices and employment/unemployment. In that sense, we classify this contribution as methodological rather than theoretical. Notably, we found a very strong correlation between the values of the PCs and those of the labor market indicators. We also found robust evidence of Granger causality in both directions.

The Uruguayan case contributes to the analysis of price formation in emerging economies and is interesting for the following reasons: i) the unique dataset employed; ii) the time-series PCA approach's novelty; and, iii) the relevance for analyzing inflation-expectations models and its anchor for central banks.

We found a positive and statistically significant small relationship between sales and unemployment. The firms used sales in the lower part of the business cycle to adjust prices. Therefore, we contributed to the literature on the relevance of price rigidity to macroeconomic dynamics. Our results indicated that sales do not alleviate much of the rigidity in an economic recession. Also, we found that all the sectors shared a common correlation structure, captured by the fact that the first principal component of each sector was strongly correlated with both employment and unemployment (especially for the food, fruits and vegetables, and personal care categories).

The rest of the paper is organized as follows: Section 2 explores the literature on price stickiness and its relationship with microeconomic and macroeconomic variables. Section 3 describes the data used, and Section 4 explains the methodological aspects of the paper and shows the results. Finally, Section 5 concludes the paper.

2. Literature review

Based on the increased availability of retailer micro price level data, the literature has adopted a micro approach to traditional macroeconomics topics like the real effects of monetary policy, price stickiness, and the relationship between inflation and unemployment. The discussion moved from the macrodata analysis to the study of microdata. Nakamura and Steinsson (2008), for example, use the consumer price index (CPI) and the producer price index (PPI) from the US Bureau of Labor Statistics (BLS) for the period 1988–2005 to study price stickiness. Their results show that regular prices last between eight and 11 months, after excluding sale prices. Sales are an essential source of (downward) price adjustment. Moreover, roughly one-third of price changes, excluding sales, are price decreases. Price changes are highly seasonal, mainly in the first quarter.

Glandon (2018) used scanner data to investigate sales and their role in aggregate price adjustments. This paper shows that sales are positively correlated with the local unemployment rate during recessions. According to the author, the CPI indexes used to deflate nominal consumption expenditures do not fully account for variation in sales.

In addition, the costs of permanently updating information lead to inattentive agent models for explaining microeconomic price rigidity. Two of the most relevant models of inattentive agents are sticky information (Mankiw (2002)) and those of noisy information (Sims (2003)). Golosov and Lucas Jr. (2007) built a model based on a monetary economy in which repricing of goods is subject to a menu cost (fixed cost) along with the presence of idiosyncratic shocks. This model is used to examine the behavior of Phillips curves by analyzing the correlations between inflation rates and levels of production and employment. Their main finding is a small and temporary response of real variables such as output, employment, and prices to an increase in nominal wages. The real effects are less persistent than those in other economies with time-dependent pricing are.

Similarly, Kehoe and Midrigan (2015) build a menu-cost model in which firms can change their prices either permanently (from their regular price) or temporarily (sales). The timing and magnitude of sales are fully responsive to the state of the economy. The

¹ The principal components (PCs) are linear transformations of the original set of variables and are uncorrelated and ordered so that the first few components carry most of the variation of the original dataset.

authors find that sales price change contribution is small as compared to the response of aggregate prices to monetary shocks. In other words, sales have a small long-run impact on the aggregate price level. This result is because sales price changes are transitory.

Nakamura and Steinsson (2013) review and discuss evidence on price rigidity from the macroeconomics literature. They find that fiscal stimulus, taxes, and increased uncertainty are potential sources of variation in demand. In addition, the considerable heterogeneity in the frequency of price changes across sectors has implications regarding movements in relative prices and relative inflation rates across sectors. They explain that sales must be treated separately to analyze the responsiveness of the aggregate price level to various shocks because i) sales are highly transitory; ii) retailers have an incentive to stagger the timing of sales; and iii) sales must be unresponsive to macroeconomic shocks. Firms' decisions to have sales may be independent of macroeconomic conditions. In the first case, sales are more independent of macro conditions than regular price changes are. According to Coibion et al. (2015), the frequency and size of sales fall when unemployment rates rise. In addition, when the unemployment rate increases, households substitute more of their expenditures with low-price retailers, consistent with the significant expenditure reallocation across retailers by households.

Furthermore, Eichenbaum et al. (2011) assess the importance of nominal rigidities with weekly data as well as the implications of price changes. They find that nominal rigidities are important and take the same trend as reference prices and costs do. They concluded that reference prices have an average duration of one year. A retailer chooses a reference price duration for each product to keep its markup within specific bounds that are similar among different products.

More related to our study, Coibion et al. (2015) find that prices paid by consumers in the US fall with unemployment. The authors use micro-data of prices and quantities sold (the mechanism is a substitution to cheaper goods and/or cheaper stores). They find that sales do not play an important role and are unrelated to unemployment. However, they conclude that "a 2-percentage-point rise in the unemployment rate lowers inflation in effective prices by 0.2 to 0.3 percentage points relative to inflation in posted prices for a given UPC." In the 2008 crisis, unemployment rose five percentage points, implying that the reported official inflation was overestimated by at least 0.5 percentage points (the inflation target was 2%). However, Gagnon et al. (2017) find that the results of Coibion et al. (2015) are explained by the data management and, in particular, the censorship of price changes greater than 8%, which was intended to mitigate the effect of outliers (nonstandard methodological choices). They conclude that the substitution effect is not so important.

Using a different price base (CPI) for the US and UK, Kryvtsov and Vicent (2021) find that sales are countercyclical. That is, sales increase with unemployment.Note that the CPI generally does not capture an effect of sales. Moreover, Anderson et al. (2017) find that sales do not respond to economic shocks, as captured by the local unemployment rate. Therefore, the relationship between sales and unemployment is an open and relevant question to answer empirically.

We make tow contributions. First, we use microdata with self-reported sale; therefore, we do not need an algorithm to identify them. Second, we apply a novel time-series PCA to study the relationships between sales and unemployment.

3. Data

The available database is a rich unbalanced weekly panel that includes 23,902 price products from August 5th, 2014, to December 25th, 2019. Not all products appear all the time; there are 2,759,261 observations (with almost 10,000 products constantly appearing throughout the period). In 2019, for example, there were 14,274 products. If a product does not appear in the database in a given period, that means it was not in stock for sale.

The data source is one store in the capital city (Montevideo) from a major retail business in Uruguay that targets the average Uruguayan household.² According to a report from the Ministry of Economy and Finance (MEF, 2020), this supermarket chain business is the largest retailer in the country, with a market share of 42% of total sales in 2019. The data are updated on a regular weekly basis, and it can also be scraped through the supermarket website. All products were classified into eight sectors or categories, with the most common products being food. The categories are:

- Food
- · Fruits and vegetables
- · Non-alcoholic drinks (sodas, water, etc.)
- Alcoholic drinks
- Cleaning products
- · Personal care products
- · Tobacco products
- Other products³

Figure 1 shows the distribution of observations by product category. The food category is the most important, with almost half of the sample, followed by personal care. The shares of product categories have not changed much overtime. The only relevant change was the growing trend in the food and other products categories which comprise about half of the sample.

Table 1 shows summary statistics. The median annualized yearly price change for all the products in the sample was 7.41%, very close to the mean inflation of 8.03%. The tobacco category had the highest price increase in the sample. The unemployment rate varied from a minimum of 5.85 percentage points to a maximum of 9.92 percentage points in the analyzed period.

² This chain follows a uniform price policy in Montevideo.

³ This category contains heterogeneous products such as shoes, lamps, batteries, newspapers, books, school supplies, pet food, and kitchen items.



Fig. 1. Distribution of product categories. Source: supermarket data, authors' classification.

Variable	Ν	Mean	Median	St. Dev.	Min	Max
A.Annualized % price changes						
All goods	463,280	7.41	6.90	9.86	-81.97	350
Food	253,001	7.13	6.38	9.78	-81.97	330.97
Cleaning	37,919	7.39	7.38	8.34	-72.46	350
Non-alcoholic drinks	19,711	6.49	6.38	8.33	-57.14	69.40
Alcoholic drinks	36,533	7.00	6.92	7.45	48.70	151.61
Fruits and vegetables	11,471	8.70	0	25.06	-63.96	273.03
Other	17,023	7.01	6.84	6.88	-42.15	81.96
Personal care	86,481	8.47	8.47	8.72	-75.28	192.92
Tobacco	1141	12.90	12.50	7.21	0.00	35.71
B.Other variables						
Mean sales	685,343	0.067	0	0.21	0	1
CPI (annualized % variation)	65	8.03	8.10	1.33	5.24	11.00
Unemployment %	65	7.90	7.93	0.79	5.85	9.92
Employment %	65	58.20	58.08	1.22	55.63	60.74

Table 1	
Descriptive	statistics.

Besides the product description, price, and date, a binary variable indicates whether the product is on sale according to the supermarket. This variable is relevant because the literature typically has required an algorithm to define sales, as in Nakamura and Steinsson (2008). In our case, we do not require the use of an algorithm. A sale does not necessarily mean reducing the list price, in our sample. For example, the item might have been included in a mailing list or bundled with another product. There is no consensus in the literature on what defines a sale; for instance, some commercial strategies such as bundling and price discounting are sales even though no price have been reduced. In our data, the store reports if the product is on sale; therefore, we do not require the use of arbitrary algorithms to define a sale. We compute sales as the fractions of weeks in a month that a product is on sale. On average, 6.7% of the products were on sale each month.

Figure 2 shows the percentage of products on sale in the sample period. The unemployment (employment) rate in the period ranged from 5.85% (55.63%) to 9.92% (60.74%), with a median value of 7.93% (58.08%).

Figure 3 shows that around 4.7% of products changed their price within a month (3.4% up and 1.2% down). In addition, sales and all changes showed strong seasonality. In 2015 and 2016, there were two price change outliers (11% and 16%, respectively). Afterward, most of the time, this price change was closer to 4%.

As shown in Fig. 4, on average, 10% of the products were on sale in June. Similar peaks appeared in November, and a minimum of 2.5% of products were on sale in January. On the one hand, regarding upward price changes, the share of products was almost 6% in February and, nearly 5% in July and October. On the other hand, price reductions peaked at the same time as sales did (in June), with 1.7% of the products. These seasonal variations in June and November could be explained by pre-Christmas shopping and the fact that employees in Uruguay are entitled to so-called "13th" bonuses by law, with half paid in June and the rest in December.

Among only the products on sale, only 13% refers to price changes (9.2% refer to a price decrease and 3.8% to a price increase). As the following figure shows, price changes to products on sale go side by side with price decreases. However, when we remove sales, price decreases practically disappear (see Fig. 5).



Fig. 2. Monthly share of products labeled as on sale. Source: supermarket data.



Fig. 3. Monthly share of products whose price changed. Source: supermarket data.

Some products are linked to the official Consumer Price Index (CPI). These products represent 12.1% of the total (14.3% considering only products in 2019).

We consider employment and unemployment data from the Uruguayan National Household Survey (ECH), conducted by the National Institute of Statistics (INE). The ECH is administered throughout the year to generate an accurate picture of the urban Uruguayan employment situation and its socio-economic characteristics. We used data from 2014 to 2019 for Montevideo, the capital of Uruguaya. Fig. 6 shows, from August 2014 to December 2019, the unemployment rate rose, and the employment rate persistently fell.



Fig. 4. Seasonality of the share of products whose price changed. Source: supermarket data.



Fig. 5. Monthly share of products, on sale or not, whose price changed. Source: supermarket data.

There is seasonality in these variables, especially in the unemployment rate (see Fig. 7). For example, unemployment grew most in the last two quarters in the period considered. Therefore, we performed a seasonal adjustment for the empirical analysis. Figs. 8a and 8b analyze each product category's price dispersion with and without sales. We found no statistically significant differences between the analyses with and without sales except in the "other" product category, which has a heftier price dispersion with sales. We found other slight differences in the fruits and vegetables and the personal care categories. Dispersion is important to explain consumer behavior and consumer search costs. For example, according to Stigler (1961), Carlson and McAfee (1983), and Janssen and Moraga (2000), the level of price dispersion is positively related to the number of suppliers.

4. Methodology and results

4.1. Sales and unemployment

We estimated the following fixed-effects panel regression to analyze the relationship between sales and unemployment:

 $sale_{i,t} = \alpha_i + \alpha_t + \beta * unemployment_{t-3} + \varepsilon_{it}$



Fig. 6. Percent change in employment and unemployment rate in Montevideo, Uruguay. Source: Uruguayan National Household Survey (ECH), National Institute of Statistics (INE).



Fig. 7. Mean of percent change in employment and unemployment rate by quarters. Source: Uruguayan National Household Survey (ECH), National Institute of Statistics (INE).

where $sale_{i,t}$ is the probability that a product *i* was labeled as on sale by the supermarket in month *t* (we computed sale as the fractions of weeks in a month that a product was on sale). The right side of the equation features fixed effects for the product (*i*) and time (*t*), and the unemployment index lagged by three months (because the index is released three months later). Because of the correlation of the error term, we clustered the standard errors at the product and time levels.

Table 2 shows a positive and statistically significant relationship between sales and unemployment (lagged and current). As the economy worsens and unemployment increases, the supermarket uses sales to a greater extent as a mechanism for price adjustment and to stimulate revenue in an adverse scenario. In this way, sales undo the effects of price rigidities in terms of monetary non-neutrality. This increase, although statistically significant, is relatively small. A one-percentage-point increase in the lagged unemployment rate raises the probability of a sale by 0.006 and 0.014 for the case of current unemployment. To quantify this effect, remember



Fig. 8. Price dispersion with and without sales. Source: Uruguayan National Household Survey (ECH), National Institute of Statistics (INE).

	Dependent variable:	
	Probability of being on s	ale
	(1)	(2)
Unemployment ₁₋₃	0.006*** (0.001)	
Unemployment,		0.014*** (0.001)
Observations Adjusted R ²	685,343 0.253	685,343 0.239

 Table 2

 Sale probability regression with product- and time-fixed effects.

Controls: FE (products and time). Clustered errors at the product and time levels in parentheses. *Note:* p<0.1; p<0.05; p<0.01.

that the average probability of sales is 0.067, so a one-percentage-point increase in the unemployment rate raises sales by 11.66% = ((0.067/0.006)-1)*100.

This result contrasts Coibion et al. (2015), who found that sales are not relevant from a macroeconomic perspective and not related to the business cycle. Moreover, they found that sales are largely acyclical. Our positive and statistically significant effect of unemployment on sales remained when we used current unemployment instead of three-month lagged unemployment. In this case, the effect double.

As Coibion et al. (2015) point out, the inclusion of time-fixed effects should eliminate endogeneity because of the simultaneous response of prices and unemployment to aggregate shocks. Including time-fixed effects allows a causal interpretation of the results. Although our estimates were statistically significant, the economic magnitude of the effect remained relatively low.

In addition to using time- and product-fixed effects, we used instrumental variables with one-period-lagged unemployment as an instrument for current unemployment to avoid endogeneity. Table 3 show this instrumental variable estimation. Our results revealed shows that our instrument was relevant and statistically significant from the first stage. The second stage showed a positive and statistically significant relationship between unemployment and sales.

In Table 4, we controlled by the interaction between product and quarter as a robustness check. We found that our instrument was still relevant, and there was a positive and statistically significant relationship between sales and unemployment.

We also estimated the same panel regression using price change probability as the dependent variable instead of sale probability. We observed a negative and statistically significant relationship between the probability of price change and unemployment

(lagged and current). This result indicates that price changes become infrequent in the worst stage of the business cycle (see Table 5). We also estimated Eq. 1 for each product category in our sample. Table 6 shows that the results remained the same for most products. Interestingly, we observed a negative and statistically significant relationship between sales and unemployment for the cleaning product category. This result could indicate that cleaning items are procyclical. One possible explanation may be that people stay in their homes for longer periods when unemployment rises and are more attentive to cleaning them. Similarly, as it contains home products supplies, the "other" category behaved in the same way as cleaning products.

Table 3		
Instrumental	variables	estimates.

	Dependent variable:		
	Probability of being on sale		
	(1)	(2)	
Unemployment _{t-3}	0.022****		
	(0.001)		
Unemployment,		0.016***	
		(0.001)	
1st F-stat	40.94***	38.15***	
Observations	685,343	685,343	
Adjusted R ²	0.016	0.014	

Controls: FE (products and time). Clustered errors at the product and time levels in parentheses. *Note:* *p<0.1; **p<0.05; ***p<0.01. Instrument: one-period-lagged unemployment.

Table 4

Instrumental variables estimates: Robustness check. Product x quarter fixed effects.

	Dependent variable:		
	Probability of being on sale		
	(1)	(2)	
Unemployment _{t-3}	0.013*** (0.0005)		
Unemployment,		0.008*** (0.0005)	
1st F-stat	13.67***	10.11***	
Observations Adjusted R ²	685,343 0.048	685,343 0.055	

Controls: FE (products interacted with quarter). Clustered errors at the product and quarter levels in parentheses. *Note:* *p<0.1; **p<0.05; ***p<0.01. Instrument: one-period-lagged unemployment.

Table 5

Regression for price change probability with product- and time-fixed effects.

	Dependent variable: Probability of price change		
	All products	Without sales	
Unemployment _{t-3}	-0.009***	-0.010***	
	(0.0003)	(0.0003)	
Unemployment,	-0.008***	-0.011***	
	(0.003)	(0.004)	
Observations	685,343	668,624	
Adjusted R ²	0.146	0.123	

Controls: FE (products and time). Clustered errors at the product and time levels in parentheses. *Note:* p<0.1; p<0.05; p<0.01.

Table 6

Regressions for the probability of being on sale by category, with unemployment.

	Dependent	variable:					
	Probability of being on sale						
	Food	Pers.care	Cleaning	Alc. drinks	Non-alc. drinks	Fruit/veg	Other
Unemployment _{t-3}	0.008*** (0.001)	0.004** (0.001)	-0.006*** (0.002)	0.010*** (0.002)	0.023*** (0.002)	0.009*** (0.002)	-0.003** (0.002)
Obs. Adj.R ²	366,936 0.232	133,807 0.309	55,294 0.268	49,059 0.197	28,670 0.215	18,722 0.322	31,243 0.414
df=	355,581	128,845	53,274	47,749	27,691	17,886	28,401

Controls: FE (products and time). Clustered errors at the product and time level in parentheses. *Note:* $^{*}p<0.1$; $^{**}p<0.05$; $^{***}p<0.01$.

Table 7

Regressions for the probability of being on sale for all and by category with employment.

	Dependent v	variable:						
	Probability	of being on sa	ale					
	All	Food	Pers.care	Cleaning	Alc. drinks	Non-alc. drinks	Fruit/veg	Other
Employment _{t-3}	-0.004*** (0.001)	-0.006*** (0.0005)	-0.003** (0.001)	0.004*** (0.001)	-0.007*** (0.001)	-0.016*** (0.002)	-0.006*** (0.002)	-0.002 (0.001)
Obs. Adj.R ² df=	685,343 0.253 661,377	366,936 0.232 355,581	133,807 0.309 128,845	55,294 0.268 53,274	49,059 0.197 47,749	28,670 0.215 27,691	18,722 0.322 17,886	31,243 0.414 28,401

Controls: FE (products and time). Clustered errors at the product and time levels in parentheses. *Note:* *p<0.1; **p<0.05; ***p<0.01.

Table 8

Regressions for the probability of count sale and count price change with unemployment.

	Dependent variable:				
	Number of weeks on sale in the month	Number of price changes in the mo			
	All products	All products	Without sales		
Unemployment _{t-3}	0.040*** (0.002)	-0.011*** (0.001)	-0.012*** (0.001)		
Observations Adjusted R ²	685,343 0.230	685,343 0.141	668,624 0.116		

Controls: FE (products and time). Clustered errors at the product and time levels in parentheses. *Note:* $^{*}p<0.1$; $^{**}p<0.05$; $^{***}p<0.01$.

Table 9

Regression for the sale probability with product- and time-fixed effects Sample of products in stock in more than half of the periods.

	Dependent variable:				
	Probability of being on sale	Probability of price	change		
	All products	All products	Without sales		
Unemployment ₁₋₃	0.008*** (0.001)	-0.0094*** (0.00025)	-0.0113*** (0.00027)		
Observations Adjusted R ²	529,085 0.223	529,085 0.1505	514,216 0.1208		

Controls: FE (products and time). Clustered errors at the product and time levesl in parentheses. *Note:* $^{*}p<0.1$; $^{**}p<0.05$; $^{***}p<0.01$.

One concern with the previous results is that individuals can shift from being employed to being out of the labor force (inactive) during a recession. For this reason, the unemployment rate alone is not a good measure of economic conditions. Therefore, as a robustness check, we estimated the sales regression against the employment rate (defined as the number of employed people divided by the total labor force). Table 7 shows the results of using seasonally adjusted employment data with three lags instead of unemployment alone. Contrary to our previous analysis, the "other" category yielded a statistically non-significant relationship between sales and employment. This could be explained by the heterogeneity of this category's products (residual category).

As an additional robustness check, we replaced the probability of sale with the number of weeks the product was on sale as a dependent variable. Table 8 shows the relationship between lagged unemployment and the number of weeks each product type was on sale. Our previous results held as we noted a positive and statistically significant relationship between unemployment and sales. Regarding the relationship between lagged unemployment and the number of price changes in a month, we again observed a negative and statistically significant relationship when considering all products without sales.

Because not all products are available all the time, we estimated Eq. 1 for the subsample of 9626 products in stock in more than half of the periods as a final robustness check. The results in Table 9 are similar to our previous findings.

4.2. Correlation and Granger causality analysis

In this section, we describe the price correlation structure of the products introduced above. Given their partition in terms of sectors (e.g., food, drinks), such products are naturally organized in clusters. We reasonably expected correlations between prices to be stronger among products belonging to the same clusters. This structure naturally lends itself to dimensionality reduction, which we performed using PCA. In a nutshell, extracted time series data (the principal components) from each sector. Their dynamics over

Table 10

Summary statistics of the first two PCs of each sector. n_+ denotes the fraction of positive components in the corresponding eigenvectors.

	1st PC		2nd PC	
	<i>n</i> ₊	% of var. explained	<i>n</i> ₊	% of var. explained
Food	72.3%	45.6%	56.4%	11.6%
Pers. care	68.8%	43.2%	50.8%	11.7%
Cleaning	70.3%	43.9%	55.2%	10.3%
Alc. drinks	68.1%	55.0%	55.2%	10.5%
Drinks	68.1%	39.1%	53.8%	12.1%
Fruits and veg.	75.5%	31.2%	55.1%	12.1%
Other	60.2%	34.4%	68.1%	16.1%

Table 11

Pearson correlation between employment and unemployment rates and the value of the first PC of each sector in the final week of the month of the indicators' publication.

	Employment	Unemployment
Food	0.920***	-0.796***
Pers. care	0.917***	-0.807***
Cleaning	0.922***	-0.804***
Alc. drinks	0.907***	-0.768***
Drinks	0.913***	-0.797***
Fruits and veg.	0.882***	-0.747***
Other	0.901***	-0.802***

Note: *p<0.1; **p<0.05; ***p<0.01.

time represent the price dynamics of all or some of a sector's products. Then, we tested whether such time series displayed statistically significant correlations or causal relationships with our macroeconomic variables of interest.

To the best of our knowledge, this approach to price rigidity analysis is entirely novel. PCA is a widely used tool to explain the variance of multivariate datasets through interpretable synthetic variables (principal components) that can be ranked in terms of relative importance. However, PCA is not frequently used in the time domain, which is key to our analysis. We compressed each sector's product price dynamics over hundreds or thousands of time series into just *two* time series, which in all cases accounted for more than half of each sector's price variance. Appendix A provides a short overview of PCA in the temporal domain, which we extensively leveraged.

The first two columns of Table 10 show summary statistics for all sectors' first principal components (PCs) in the price-time series. We report the fraction n_+ of positive components in the first two eigenvectors of each sector's correlation matrix (as explained in Appendix Appendix A, quantifies the fraction of variables that share a positive correlation with the corresponding PC) and the fraction of variance explained by the corresponding PC. As seen from the latter number, the first PC of each sector explained a considerably large proportion of the variance of its price dynamics, ranging from more than 30% to 55% in the case of alcoholic drinks. Furthermore, the n_+ values– all abundantly greater than 50% – showed that the first PC was a clear source of positive correlation among most product prices in each sector.

Our results showed that more than *half* of the variance in price dynamics for each sector can be explained by the first two PCs, suggesting that such quantities may hold relevant information concerning our macroeconomic variables of interest. Table 11 depicts the correlation between monthly employment status and the values of each sector's first PC in the final week of the same month. We observed a remarkably strong positive (negative) correlation between employment (unemployment) and the first PCs (p < .01 in all cases). Correlations with second PCs were not statistically significant (p > 0.1 in all cases) and are therefore not reported. The positive correlation among all sector's first PCs and employment is visually clear from Fig. 9, in which we plotted all standardize variables' time evolution.

The above results clearly hint at a rather strong relationship between employment / unemployment status and the price dynamics of the sectors we considered, as explained by the first PC. We further investigated this by measuring causal interactions in the Granger sense. In Table 12 we report the results of Granger causality tests, which determine whether variation in one variable is explanatory of future variation in another variable with a certain time lag (for a complete description of the test, see Granger (1969)). Here, we tested whether employment / unemployment Granger-caused each sector's first two PCs in the final week of the second month after their values were published. We find substantial Granger causality across the board. In particular, we found that employment Granger-caused the first two PCs of all sectors except for "other" with different levels of statistical significance In addition, we found that unemployment Granger-caused the first PCs in the alcoholic drinks and fruits and vegetables sectors, and the second PCs of all sectors except for food, and other. We also find robust evidence of reverse causal relationships by testing whether the first two PCs of each sector Granger-caused both indicators except unemployment in the following month (see Table 13). We find that the first PCs of each sector Granger-caused both indicators except unemployment in the case of the 'other' sector. Conversely,



Fig. 9. Time evolution of the PCs of the seven product sectors (grey solid lines) and employment (purple dots and dashed line). Employment time series standardized for comparison. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.).

Table 12

F-statistics of Granger causality tests between employment and unemployment rates and first and second PCS in the final week of the second month after indicators publications.

	1st PC		2nd PC	
	Employment	Unemployment	Employment	Unemployment
Food	5.07***	2.19	5.57**	2.48
Pers. care	6.46**	2.71	5.27**	6.91***
Cleaning	5.92***	1.45	6.98**	5.08***
Alc. drinks	6.47**	8.07***	1.80***	1.50***
Drinks	3.81**	9.86	1.59***	7.32***
Fruits and veg.	1.75***	1.80***	1.79***	8.15***
Other	0.16	8.69	2.52	1.67

Note: *p<0.1; **p<0.05; ***p<0.01.

Table 13

F-statistics of reverse Granger causality tests between employment and unemployment rates and first and second PCs in the final week of the month prior to publication of the indicators.

	1st PC		2nd PC	
	Employment	Unemployment	Employment	Unemployment
Food	23.7***	10.6***	4.17	2.67
Pers. care	20.1***	11.7***	0.14	0.88
Cleaning	26.3***	11.4***	2.11	0.87
Alc. drinks	10.7***	8.11***	0.31	1.02
Drinks	22.0***	9.97***	0.14	0.87
Fruits and veg.	13.2***	6.08	0.20	1.10
Other	10.4***	9.66***	6.98***	6.77***

Note: *p<0.1; **p<0.05; ***p<0.01.

the 'other' sector was the only one for which we detected a statistically significant causal relationship between the second PC and both employment and unemployment in the following month.

Appendix Appendix B (see Tables B.14 and B.15) shows the results obtained when testing for direct and reverse Granger causality with four additional weeks of time lag. We found that the Granger causality from both employment and unemployment to the first PC faded away almost without exception, whereas it remained fairly strong with respect to most sectors' second PCs. Conversely, we found that each sector's PCs still Granger-caused the indicators, and the relationship remains statistically significant even for greater time lags (see Tables B.14 and B.15). Similar results are obtained when testing for Granger and reverse Granger causality between employment status and the average weekly values of the first and second PCs computer over months before and after indicators' publication (see Tables B.16 and B.17).

5. Conclusions

We used a rich weekly price database from the largest supermarket chain in Uruguay to analyze the relationships among prices, sales, and business cycle conditions captured by the unemployment / employment rate. Our results showed a statistically significant but small positive relationship between unemployment and prodcut categories' price dynamics. In this way, sales undo part of the effects of price rigidities in terms of monetary non-neutrality. As this effect is relatively small, sales do not alleviate rigidities in an economic recession.

Regarding product categories, food products, alcoholic drinks, non-alcoholic drinks, and fruits and vegetables displayed strong and positive statistically significant relationships between the probability of being on sale and unemployment rates. On the other hand, food products, cleaning, alcoholic drinks, non-alcoholic drinks, and fruits and vegetables all displayed and negative statistically significant relationships between the probability of being on sale and employment rates.

We also performed a novel time-series PCA and found that all product categories shared a mutual correlation structure. The most statistically significant correlation occurred between employment variation and the first principal component for each product category. We also observed substantial Granger causality between unemployment rates and the first principal component of the alcoholic drinks and fruits and vegetable sectors.

Declaration of Competing Interest

There is no conflict of interest.

Appendix A. Principal component analysis

This section provides a quick overview of PCA in the time domain, which we used extensively in our correlation and Granger causality analyses. Suppose we are interested in studying the statistical properties of N time series, each one made of T observations. Let us collect their standardized data (i.e., zero mean and unit variance) x_{it} - with i = 1, ..., N, and t = 1, ..., T - in an $N \times T$ matrix **X**, which we can then use to construct the $N \times N$ Pearson correlation matrix $\mathbf{C} = \mathbf{X}\mathbf{X}^{\mathrm{T}}/T$. By definition, such a matrix is symmetric and positive definite. Hence, it yields N non-negative eigenvalues $\lambda_1 \ge \lambda_2 \ge ... \ge \lambda_N \ge 0$. The corresponding eigenvalue problem can be written as

$$\mathbf{C}\mathbf{V}^{(i)} = \lambda_i \mathbf{V}^{(i)} \tag{2}$$

where $\mathbf{V}^{(i)} = (V_1^{(i)}, V_2^{(i)}, \dots, V_N^{(i)})$ is the normalized eigenvector for the *i*-th eigenvalue. Since **C** is symmetric, the eigenvectors $\mathbf{V}^{(i)}$ are mutually orthogonal (i.e., $\sum_{j=1}^{N} V_j^{(i)} V_j^{(\ell)} = 0$ for $i \neq \ell$). The main point about PCA is that the set of *N* time series x_{it} can be mapped onto a set of *N* exactly uncorrelated standardized time

series $e_{i,r}$, called principal components (PCs). This is achieved with the following linear transformation:

$$e_{it} = \frac{1}{\sqrt{\lambda_i}} \sum_{j=1}^{N} V_j^{(i)} x_{jt},$$
(3)

where

$$x_{it} = \sum_{k=1}^{N} \sqrt{\lambda_k} V_i^{(k)} e_{kt}.$$
(4)

By exploiting eigenvector orthogonality one can immediately verify that the new variables introduced in Eq. (4) are indeed uncorrelated:

$$\frac{1}{T}\sum_{i=1}^{T}e_{it}e_{jt}=\delta_{ij},$$
(5)

where $\delta_{ij} = 1$ if i = j and $\delta_{ij} = 0$ otherwise.

All in all, Eq. (4) shows that the result of the PCA mapping is to decompose the time evolution of each time series x_i into N uncorrelated contributions whose standard deviation is proportional to the square root of the eigenvalues of the empirical correlation matrix. Therefore, the ratios λ_i/N quantify the fraction of the overall variance in the original data explained by the *i*-th PC.

Now, suppose that a few eigenvalues (e.g., the first *M*) are much greater than the remaining ones. Then, by virtue of Equation (4), one could approximate each x_i as

$$x_{it} \sim \sum_{k=1}^{M} \sqrt{\lambda_k} V_i^{(k)} e_{kt}.$$
 (6)

In the limiting case of a single eigenvalue being much larger than any other ($\lambda_1 \gg \lambda_i$ for i = 2, ..., N) one could eventually approximate all variables using the first PC e_1 :

$$x_{it} \sim \sqrt{\lambda_1} V_i^{(1)} e_{1t}. \tag{7}$$

Despite being rather crude, the above approximation is a useful first step to understanding multivariate time series' collective dynamics. In particular, inspecting the first eigenvector's components $(V_1^{(1)}, \ldots, V_N^{(1)})$ provides relevant insight into the role played by the first PC. In fact, when most components $V_i^{(1)}$ share the same sign, the first PC e_1 acquires a clear meaning as a source of positive correlation in the system, as it "drives" most variables x_i in the same direction.

If we extend the simple approximation in Eq. (7) to include the second PC, we obtain

$$x_{it} \sim \sqrt{\lambda_1} V_i^{(1)} e_{1t} + \sqrt{\lambda_2} V_i^{(2)} e_{2t}.$$
(8)

Analogous to the above consideration, inspecting the second eigenvector's components $(V_1^{(2)}, \dots, V_N^{(2)})$ determines the interpretation of the second PC as a source of additional correlation with respect to the correlations encoded in the first PC. Similar considerations apply to all following PCs.

Appendix B

Additional tables on Granger causality

Table B1

F-statistics of Granger causality tests between employment and unemployment rates and first and second PCs values in the final week of the third month after the indicators' publication.

	1st PC		2nd PC	
	Employment	Unemployment	Employment	Unemployment
Food	3.74	0.31	9.95***	5.71***
Pers. care	2.46	0.91	16.3***	10.5***
Cleaning	3.75	0.25	12.2***	4.35
Alc. drinks	3.35	0.14	21.6***	13.1***
Drinks	5.13***	1.73	20.3***	6.03***
Fruits and veg.	3.82	0.97	6.59***	4.37
Other	3.62	0.68	1.74	0.75

Note: *p<0.1; **p<0.05; ***p<0.01.

Table B2

F-statistics of reverse Granger causality tests between employment and unemployment rates and first and second PCs in the final week of the second month before the indicators' publication .

	1st PC		2nd PC	
	Employment	Unemployment	Employment	Unemployment
Food	21.2***	8.04***	3.19	5.45***
Pers. care	11.9***	7.93***	2.47	4.61
Cleaning	23.8***	8.14***	8.58**	5.02***
Alc. drinks	16.1***	7.33***	0.66	5.49***
Drinks	10.9***	7.74***	5.37**	5.62***
Fruits and veg.	11.8***	6.02***	0.60	3.61
Other	15.5***	10.0***	1.57	4.65

Note: *p<0.1; **p<0.05; ***p<0.01.

Table B3

F-statistics of Granger causality tests between average weekly values of the first and second PCs in a month and the following month's employment and unemployment .

	1st PC		2nd PC	
	Employment	Unemployment	Employment	Unemployment
Food	2.67	1.21	3.51	1.46
Pers. care	3.94	1.67	8.93***	10.7***
Cleaning	4.75	1.22	9.22***	3.52
Alc. drinks	2.47	2.27	6.46***	7.36***
Drinks	3.72	0.19	9.77***	7.07
Fruits and veg.	2.99	1.05	4.09	1.71
Other	5.68	1.37	16.2***	9.19***

Note: *p<0.1; **p<0.05; ***p<0.01.

Table B4

F-statistics of Granger causality tests between employment and unemployment rates and the following month's average weekly values of the first and second PCs .

	1st PC		2nd PC	
	Employment	Unemployment	Employment	Unemployment
Food	20.2***	11.3***	3.07	0.88
Pers. care	27.3***	13.1***	0.19	0.84
Cleaning	31.7***	12.0***	0.15	0.82
Alc. drinks	20.1***	8,33***	3.25	1.02
Drinks	26.0***	8.61***	0.14	0.84
Fruits and veg.	13.7***	7.33***	2.55	2.76
Other	24.6***	10.7***	1.21	3.05

Note: *p<0.1; **p<0.05; ***p<0.01.

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